Candidate surname	Other names
Pearson Edexcel International Advanced Level	tre Number Candidate Number
Friday 24 May 2	2019
Morning (Time: 1 hour 35 minutes)	Paper Reference <b>WPH05/01</b>
	·
Physics Advanced Unit 5: Physics from Creati	on to Collapse

## **Instructions**

- Use black ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided
  - there may be more space than you need.

# Information

- The total mark for this paper is 80.
- The marks for **each** question are shown in brackets
  - use this as a guide as to how much time to spend on each question.
- Questions labelled with an asterisk (\*) are ones where the quality of your written communication will be assessed
  - you should take particular care with your spelling, punctuation and grammar, as well as the clarity of expression, on these questions.
- The list of data, formulae and relationships is printed at the end of this booklet.
- Candidates may use a scientific calculator.

# **Advice**

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ▶







# **SECTION A**

# **Answer ALL questions.**

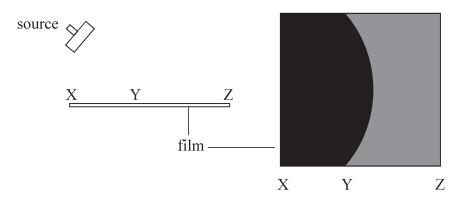
For questions 1–10, in Section A, select one answer from A to D and put a cross in the box ⊠. If you change your mind, put a line through the box ⋈ and then mark your new answer with a cross ⋈.

1	Sci	enti	sts are still working to develop a practical nuclear fusion reactor.
	Wh	nich	of the following explains why controlled nuclear fusion on Earth is difficult to achieve?
	X	A	Fusion requires very high temperatures.
	X	В	Fusion requires very high pressures.
	X	C	Fusion requires large amounts of hydrogen.
	×	D	Fusion requires strong magnetic fields.
			(Total for Question 1 = 1 mark)
2			ent used a detector and counter to determine the count rate near to a radioactive. She also measured the background count for 10 minutes.
	Wh	nich	of the following must she do to obtain an accurate value for the count rate?
	X	A	Add the background count to her count rate.
	X	В	Add the background count rate to her count rate.
	X	C	Subtract the background count from her count rate.
	X	D	Subtract the background count rate from her count rate.
			(Total for Question 2 = 1 mark)
3	The	e ze	ro on the kelvin temperature scale is known as the absolute zero of temperature.
	Wh	nich	of the following is a description of absolute zero?
	X	A	It is the lowest temperature yet reached in a laboratory.
	X	В	It is the temperature at which hydrogen liquefies.
	X	C	It is the temperature at which molecules have their lowest kinetic energy.
	X	D	It is the temperature of deep space.
			(Total for Question 3 = 1 mark)

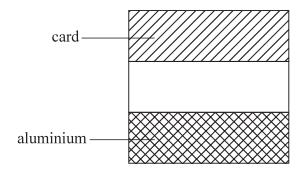


4 When exposed to ionising radiation photographic film darkens. The darkness of the film shows how much ionising radiation the film has been exposed to. A source emitting  $\alpha$ ,  $\beta$ , and  $\gamma$  radiation was placed a small distance from some photographic film in a light-tight box.

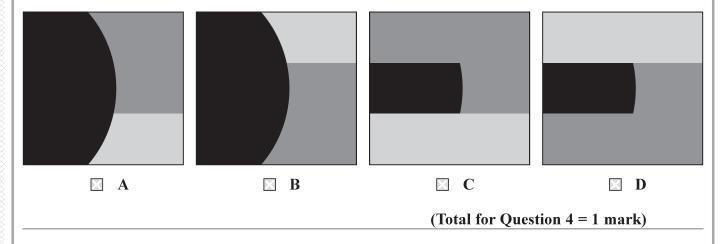
The film became darkened as shown. X, Y and Z are points on the film.



A second film is covered by strips of card and aluminium as shown.



Select the diagram that shows how the film would be darkened with these strips in place.



5 Two systems are oscillating with simple harmonic motion. The angular frequency and amplitude of each oscillating system are summarised in the table below.

	System 1	System 2
angular frequency	ω	$\frac{\omega}{2}$
amplitude	A	2.4

The maximum acceleration of system 1 is  $a_1$  and the maximum acceleration of system 2 is  $a_2$ . Which of the following expressions is correct?

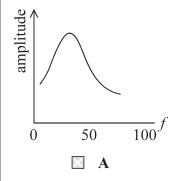
- $\blacksquare$  **B**  $a_1 = a_2$
- $\square$  **C**  $a_1 = 2a_2$
- $\square$  **D**  $a_1 = 4a_2$

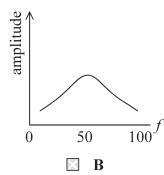
(Total for Question 5 = 1 mark)

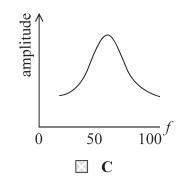
A sound engineer is designing a loudspeaker system. She wants the sound produced at a frequency of 50 Hz to be as loud as possible.

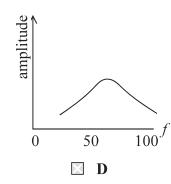
The graphs below show how the amplitude of sound produced by four loudspeaker systems varies with frequency f.

Which loudspeaker system should she choose?









(Total for Question 6 = 1 mark)

7 Earthquake-proof buildings may include materials in their structure to absorb energy from the movement of the building.

The table shows some properties of two different building materials.

	Material X	Material Y
Deforms elastically	✓	×
Deforms plastically	×	✓
Stiff	✓	✓
Strong	×	✓

Which of the following explains the most suitable material to absorb energy from the moving building?

- A Material X because it is stiff
- **B** Material X because it deforms elastically
- ☑ C Material Y because it deforms plastically
- **D** Material Y because it is both stiff and strong

(Total for Question 7 = 1 mark)

**8** Cepheid variable stars are examples of standard candles.

A standard candle is a star with a known

- **A** frequency.
- **B** luminosity.
- C radiation flux.
- **D** radius.

(Total for Question 8 = 1 mark)

**9** Astronomers are collecting data for two stars X and Y. The following observations are made.

	Star X	Star Y
parallax angle	$\theta$	$2\theta$
radiation flux	F	2F

What can be concluded about the luminosities  $L_X$  and  $L_Y$  of star X and star Y?

- $\square$  A  $L_{\rm X} > L_{\rm Y}$
- lacksquare **B**  $L_{\mathrm{X}} = L_{\mathrm{Y}}$
- $\square \quad \mathbf{C} \quad L_{\mathbf{X}} = (L_{\mathbf{Y}})^2$
- lacksquare D  $L_{
  m X} < L_{
  m Y}$

(Total for Question 9 = 1 mark)

10 Wolf 359 is the fifth nearest star to the Sun. It has a surface temperature of 2800 K and a luminosity of  $1.4\times10^{-3}~L_{\rm sun}$ , where  $L_{\rm sun}$  is the luminosity of the Sun.

Which of the following is a correct description of Wolf 359?

- A a black dwarf star
- **B** a main sequence star
- C a red giant star
- **D** a white dwarf star

(Total for Question 10 = 1 mark)

**TOTAL FOR SECTION A = 10 MARKS** 

## **SECTION B**

# Answer ALL questions in the spaces provided.

11 The air in a train carriage heats up due to the people inside the carriage.

On one journey there are 44 people in the carriage. The temperature of the air in the carriage is initially 16 °C, and rises to 28 °C.

(a) The doors and windows in the carriage are closed.

Calculate the time taken for the temperature of the air in the carriage to rise to 28 °C due to the people in the carriage.

average rate at which one person heats the air =  $85\,\mathrm{W}$  mass of air in the carriage =  $110\,\mathrm{kg}$  specific heat capacity of air =  $720\,\mathrm{J\,kg^{-1}\,K^{-1}}$ 

(3)

TD*	. 1	1	
Time	tal	ken	=

(b) Suggest why the actual time taken for the temperature to rise to 28 °C will be greater than the time you have calculated.

(1)

(Total for Question 11 = 4 marks)



12 Most scientists believe that dark matter is spread throughout the whole universe. Recent observations indicate that there may be galaxies in which there is no dark matter.												
	Discuss how the absence of dark matter in parts of the universe might affect the ultimate fate of the universe.											
		(4)										
	(Total for Question 12 = 4 marl	ks)										

A cyclist competes in a bicycle race.  Before the race a bicycle tyre contains air at a temperature of 22 °C and a pressure of 5.52 × 10° Pa.  By the end of the race, the pressure of the air in the tyre has risen to 5.60 × 10° Pa.  (a) (i) Calculate the temperature of the air in the tyre at the end of the race.  (3)  Temperature of air =	. 1		
Solution in the type has risen to 5.60 × 10 <sup>5</sup> Pa.  By the end of the race, the pressure of the air in the tyre has risen to 5.60 × 10 <sup>5</sup> Pa.  (a) (i) Calculate the temperature of the air in the tyre at the end of the race.  (3)  Temperature of air =  (ii) During the race, a small amount of air escapes from the tyre.  Explain how the value of the temperature calculated in (i) would be affected if allowance were made for this escaped air.	A cycl	ist competes in a bicycle race.	
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*(b) Explain why the pressure exerted by the air in the tyre increases as the temperature the air increases.	are of
Your answer should include reference to molecular momentum and kinetic energ	y. (4)
(Total for Question $13 = 9$	marks)

- 14 Caesium-137 is a radioactive isotope found in used fuel rods from a nuclear fission reactor. It is a beta emitter with a half-life of 30.2 years.
  - (a) Complete the decay equation

(2)

$$^{137}_{55}$$
Cs  $\rightarrow$  Ba +  $\beta$ 

(b) When it is removed from a fission reactor, a fuel rod contains  $1.36 \times 10^{24}$  nuclei of caesium-137.

Calculate the activity of the fuel rod due to the decay of the caesium-137 20 years after removal from the reactor.

1 year = 
$$3.15 \times 10^7 \,\text{s}$$

**(4)** 



Activity of fuel rod =

(Total for Question 14 = 8 marks)

(c) When caesium-137 decays it also emits gamma radiation.

Explain why the emission of gamma radiation is a more serious hazard than the emission of beta radiation.

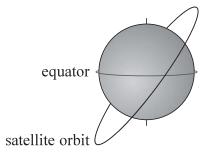
(2)

- 15 Navstar 1 was a navigation satellite placed in a circular orbit about the Earth in 1978. It was the first Global Positioning System satellite to be launched.
  - (a) (i) Show that the orbital time T for a satellite in a circular orbit of radius r about the Earth of mass M is given by

$$T^2 = \frac{4\pi^2 r^3}{GM}$$

		(3)

(ii) The plane of the satellite's orbit was inclined at an angle to the plane of the equator as shown.



Calculate the number of times that the satellite crossed over the equator each day.

radius of orbit = 
$$2.66 \times 10^7$$
 m  
mass of the Earth =  $6.0 \times 10^{24}$  kg

(3)

Number of times satellite crosses equator = ...

(b) A student calculated the increase in the potential energy of the satellite from launch to its final orbit height. He used the equation  $\Delta E_{\rm grav} = mg\Delta h$ 

Explain how the actual value for  $\Delta E_{\rm grav}$  differed from the value calculated using  $\Delta E_{\rm grav}=mg\Delta h$ 

(2)

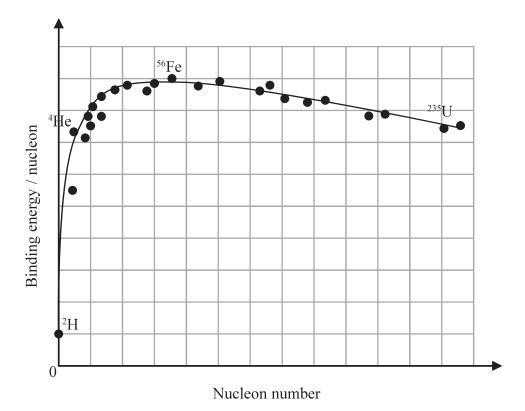
(Total for Question 15 = 8 marks)



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16 The graph shows how the binding energy per nucleon varies with nucleon number for various isotopes.



(a) (i) Explain the significance of the position of <sup>56</sup>Fe on this graph.

**(2)** 

(ii) Show that the binding energy per nucleon of  ${}^{56}_{26}$ Fe is about 9 MeV.

proton mass = 
$$1.673 \times 10^{-27}$$
 kg  
neutron mass =  $1.675 \times 10^{-27}$  kg  
mass of  $^{56}$ Fe nucleus =  $9.287 \times 10^{-26}$  kg

(4)

| <br> |
|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
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(iii) Deduce a value for the binding energy per nucleon of <sup>2</sup>H. You should use your value from (ii) and the graph.

(2)

Binding energy per nucleon =

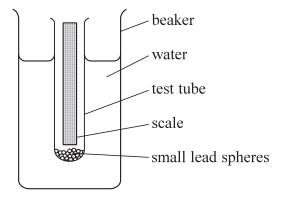
(b) The isotope uranium-235 undergoes fission into less massive isotopes.  Explain how fission of uranium-235 leads to a release of energy.	(2)
(Total for Question 16	5 = 10 marks)

- 17 A physics textbook gives the following statement about simple harmonic motion:
  - "Simple harmonic motion occurs when the acceleration of an object is proportional to the displacement from equilibrium."
  - (a) This statement is not a complete definition of simple harmonic motion.

Rewrite this statement to give a complete definition of simple harmonic motion.

**(2)** 

(b) A test tube is loaded with small lead spheres so that it floats vertically in a beaker of water as shown.

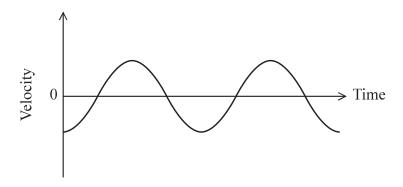


The test tube is displaced downwards and released. After release the test tube moves with simple harmonic motion.



(i)	A student uses a stopwatch to measure the period of oscillation $T$ of the test tube. Describe the procedure she should follow to obtain an accurate value for $T$ .	(3)
(ii)	The maximum displacement of the test tube from the equilibrium position is $2.0\mathrm{c}$ Calculate the maximum velocity of the test tube. $T=0.57\mathrm{s}$	
		(3)
	Maximum velocity =	

(iii) The idealised graph below shows how the velocity of the test tube varies with time.



Add to this graph to show how the acceleration of the test tube varies with time.

**(2)** 

(iv) Explain why the amplitude of the oscillation would decrease with time.

(2)

(Total for Question 17 = 12 marks)

vten's star is a low-mass	main sequence star. Scientists ha	ave recently sent signals to	
yten's star in the search		ove recessive construction	
The surface temperature	e of Luyten's star is 3150K.		
(i) Calculate the wavel	ength at which the power output i	s a maximum for this star.	
()			(2)
		Wavelength =	
(ii) The radius of Luxte	m's star is 35% of the radius of th		
	en's star is 35% of the radius of the		~
Calculate the ratio of	. 4: 41 1	on to the luminogity L of the	Caree
Calculate the fatto (	of the luminosity $L_{\rm L}$ of Luyten's st	ar to the luminosity $L_{\rm S}$ of the	Suii.
	of the Sun = $5800 \mathrm{K}$	Ü	
	ے	Ü	(2)
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(iii) The atoms in the outer regions of a star may be treated as an ideal gas. Calculate the mean kinetic energy of the hydrogen atoms in the outer regions of Luyten's star.	
	(2)
Mean kinetic energy =	
(b) The spectrum produced by hydrogen atoms in the outer regions of Luyten's star shows a strong line at a wavelength of 656.3 nm. The motion of the atoms at the surface of the star causes broadening of this line.	
*(i) Explain why the motion of the atoms in the outer regions of the star causes this wavelength to become a range of wavelengths.	(3)
*(i) Explain why the motion of the atoms in the outer regions of the star causes this	(3)
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(ii) The broadening of a spectral line of wavelength  $\lambda$  can be estimated by the equation

$$\frac{\Delta\lambda}{\lambda} = \sqrt{\frac{kT}{mc^2}}$$

where  $\frac{\Delta \lambda}{\lambda}$  is the Doppler shift in wavelength for an atom of typical speed.

T is the surface temperature of Luyten's star, m is the mass of a hydrogen atom, and c is the speed of light.

Use this equation to calculate the component of the velocity of this atom along the line of sight.

$$m = 1.67 \times 10^{-27} \,\mathrm{kg}$$

$$T = 3150 \,\mathrm{K}$$

(3)

Speed of hydrogen atoms =

\*(c) After a period of time all stars evolve and move off the main sequence.

Explain why we would expect Luyten's star to remain on the main sequence for a longer time than the Sun.

(3)

(Total for Question 18 = 15 marks)

TOTAL FOR SECTION B = 70 MARKS TOTAL FOR PAPER = 80 MARKS



# List of data, formulae and relationships

 $g = 9.81 \text{ m s}^{-2}$ Acceleration of free fall (close to Earth's surface)

Boltzmann constant  $k = 1.38 \times 10^{-23} \text{ J K}^{-1}$ 

Coulomb's law constant  $k = 1/4\pi\varepsilon_0$ 

 $= 8.99 \times 10^9 \text{ N m}^2 \text{ C}^{-2}$ 

 $e = -1.60 \times 10^{-19} \,\mathrm{C}$ Electron charge

 $m_{e} = 9.11 \times 10^{-31} \text{kg}$ Electron mass

 $1 \text{ eV} = 1.60 \times 10^{-19} \text{ J}$ Electronvolt

 $G = 6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}$ Gravitational constant

Gravitational field strength  $g = 9.81 \text{ N kg}^{-1}$ (close to Earth's surface)

Permittivity of free space  $\varepsilon_0 = 8.85 \times 10^{-12} \text{ F m}^{-1}$ 

 $h = 6.63 \times 10^{-34} \,\mathrm{J s}$ Planck constant

Proton mass  $m_p = 1.67 \times 10^{-27} \text{ kg}$ 

 $c = 3.00 \times 10^8 \,\mathrm{m \ s^{-1}}$ Speed of light in a vacuum

 $\sigma = 5.67 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$ Stefan-Boltzmann constant

Unified atomic mass unit  $u = 1.66 \times 10^{-27} \text{ kg}$ 

## Unit 1

# Mechanics

Kinematic equations of motion v = u + at

> $s = ut + \frac{1}{2}at^2$  $v^2 = u^2 + 2as$

Forces  $\Sigma F = ma$ 

> g = F/mW = mg

 $\Delta W = F \Delta s$ Work and energy

 $E_{\rm k} = \frac{1}{2} m v^2$ 

 $\Delta E_{\rm grav} = mg\Delta h$ 

#### Materials

Stokes' law  $F = 6\pi \eta r v$ 

Hooke's law  $F = k\Delta x$ 

 $\rho = m/V$ Density

Pressure p = F/A

Young modulus  $E = \sigma/\varepsilon$  where

Stress  $\sigma = F/A$ 

Strain  $\varepsilon = \Delta x/x$ 

Elastic strain energy  $E_{\rm al} = \frac{1}{2}F\Delta x$ 



# Unit 2

Waves

Wave speed  $v = f\lambda$ 

Refractive index  $_{1}\mu_{2} = \sin i / \sin r = v_{1}/v_{2}$ 

Electricity

Potential difference V = W/Q

Resistance R = V/I

Electrical power, energy and P = VI efficiency  $P = I^2 R$ 

 $P = I^{2}R$   $P = V^{2}/R$  W = VIt

% efficiency =  $\frac{\text{useful energy output}}{\text{total energy input}} \times 100$ 

% efficiency =  $\frac{\text{useful power output}}{\text{total power input}} \times 100$ 

Resistivity  $R = \rho l/A$ 

Current  $I = \Delta Q/\Delta t$ 

I = nqvA

Resistors in series  $R = R_1 + R_2 + R_3$ 

Resistors in parallel  $\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$ 

Quantum physics

Photon model E = hf

Einstein's photoelectric  $hf = \phi + \frac{1}{2}mv_{\text{max}}^2$ 

equation



## Unit 4

## Mechanics

Momentum p = mv

Kinetic energy of a

non-relativistic particle  $E_k = p^2/2m$ 

Motion in a circle  $v = \omega r$ 

 $T = 2\pi/\omega$ 

 $F = ma = mv^2/r$ 

 $a = v^2/r$ 

 $a = r\omega^2$ 

# **Fields**

Coulomb's law  $F = kQ_1Q_2/r^2$  where  $k = 1/4\pi\epsilon_0$ 

Electric field E = F/Q

 $E = kQ/r^2$ 

E = V/d

Capacitance C = Q/V

Energy stored in capacitor  $W = \frac{1}{2}QV$ 

Capacitor discharge  $Q = Q_0 e^{-t/RC}$ 

In a magnetic field  $F = BIl \sin \theta$ 

 $F = Bqv \sin \theta$ 

r = p/BQ

Faraday's and Lenz's laws  $\varepsilon = -d(N\phi)/dt$ 

# Particle physics

Mass-energy  $\Delta E = c^2 \Delta m$ 

de Broglie wavelength  $\lambda = h/p$ 

## Unit 5

Energy and matter

Heating  $\Delta E = mc\Delta\theta$ 

Molecular kinetic theory  $\frac{1}{2}m\langle c^2\rangle = \frac{3}{2}kT$ 

Ideal gas equation pV = NkT

Nuclear Physics

Radioactive decay  $dN/dt = -\lambda N$ 

 $\lambda = \ln 2/t_{1/2}$ 

 $N = N_0 e^{-\lambda t}$ 

Mechanics

Simple harmonic motion  $a = -\omega^2 x$ 

 $a = -A\omega^2 \cos \omega t$   $v = -A\omega \sin \omega t$   $x = A \cos \omega t$   $T = 1/f = 2\pi/\omega$ 

Gravitational force  $F = Gm_1m_2/r^2$ 

Observing the universe

Radiant energy flux  $F = L/4\pi d^2$ 

Stefan-Boltzmann law  $L = \sigma T^4 A$ 

 $L = 4\pi r^2 \sigma T^4$ 

Wien's law  $\lambda_{\text{max}} T = 2.898 \times 10^{-3} \text{ m K}$ 

Redshift of electromagnetic

radiation  $z = \Delta \lambda / \lambda \approx \Delta f / f \approx v / c$ 

Cosmological expansion  $v = H_0 d$ 

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