

Please check the examination details below before entering your candidate information

Candidate surname

Other names

Centre Number

Candidate Number

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Pearson Edexcel International Advanced Level

Time 1 hour 30 minutes

Paper
reference

WMA12/01

Mathematics

International Advanced Subsidiary/Advanced Level Pure Mathematics P2

You must have:

Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

**Candidates may use any calculator permitted by Pearson regulations.
Calculators must not have the facility for symbolic algebra manipulation,
differentiation and integration, or have retrievable mathematical formulae
stored in them.**

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need*.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question*.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ▶

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1. The first three terms, in ascending powers of x , of the binomial expansion of $(1 + kx)^{16}$ are

$$1, -4x \text{ and } px^2$$

where k and p are constants.

- (a) Find, in simplest form,

 - (i) the value of k
 - (ii) the value of p

(3)

$$g(x) = \left(2 + \frac{16}{x}\right)(1+kx)^{16}$$

Using the value of k found in part (a),

- (b) find the term in x^2 in the expansion of $g(x)$.

(3)



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Question 1 continued

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Q1

(Total 6 marks)



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2. A sequence is defined by

$$u_1 = 6$$

where k is a positive constant.

- (a) Find, in terms of k , an expression for u_3

(2)

$$\text{Given that } \sum_{n=1}^3 u_n = 117$$

- (b) find the value of k .

(3)



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Question 2 continued

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Q2

(Total 5 marks)



3.

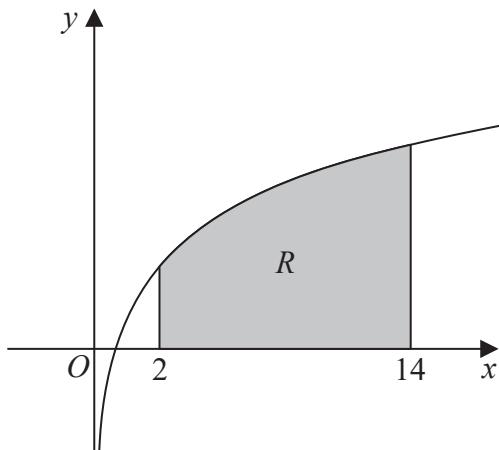


Figure 1

Figure 1 shows a sketch of part of the curve with equation $y = \log_{10} x$

The region R , shown shaded in Figure 1, is bounded by the curve, the line with equation $x = 2$, the x -axis and the line with equation $x = 14$

Using the trapezium rule with four strips of equal width,

- (a) show that the area of R is approximately 10.10

(3)

- (b) Explain how the trapezium rule could be used to obtain a more accurate estimate for the area of R .

(1)

- (c) Using the answer to part (a) and making your method clear, estimate the value of

(i) $\int_2^{14} \log_{10} \sqrt{x} \, dx$

(ii) $\int_2^{14} \log_{10} 100x^3 \, dx$

(4)



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Question 3 continued

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Q3

(Total 8 marks)



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4. $f(x) = (x^2 - 2)(2x - 3) - 21$

- (a) State the value of the remainder when $f(x)$ is divided by $(2x - 3)$ (1)

(b) Use the factor theorem to show that $(x - 3)$ is a factor of $f(x)$ (2)

(c) Hence,

(i) factorise $f(x)$

(ii) show that the equation $f(x) = 0$ has only one real root. (5)



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Question 4 continued

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Q4

(Total 8 marks)



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5. A company that owned a silver mine

- extracted 480 tonnes of silver from the mine in year 1
 - extracted 465 tonnes of silver from the mine in year 2
 - extracted 450 tonnes of silver from the mine in year 3

and so on, forming an arithmetic sequence.

- (a) Find the mass of silver extracted in year 14

(2)

After a total of 7770 tonnes of silver was extracted, the company stopped mining.

Given that this occurred at the end of year N ,

- (b) show that

$$N^2 - 65N + 1036 = 0$$

(3)

- (c) Hence, state the value of N .

(1)



Question 5 continued

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Q5

(Total 6 marks)



P 6 9 1 9 9 A 0 1 5 3 2

6. (i) The circle C_1 has equation

$$x^2 + y^2 + 10x - 12y = k \quad \text{where } k \text{ is a constant}$$

- (a) Find the coordinates of the centre of C_1 (2)

(b) State the possible range in values for k . (2)

(ii) The point $P(p, 0)$, the point $Q(-2, 10)$ and the point $R(8, -14)$ lie on a different circle, C_2

Given that

- p is a positive constant
 - QR is a diameter of C_2

find the exact value of p .

(4)



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Question 6 continued

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Question 6 continued

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Q6

(Total 8 marks)



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7. (i) A geometric sequence has first term 4 and common ratio 6
 Given that the n^{th} term is greater than 10^{100} , find the minimum possible value of n . (3)

(ii) A different geometric sequence has first term a and common ratio r .

Given that

- the second term of the sequence is -6
 - the sum to infinity of the series is 25

(a) show that

$$25r^2 - 25r - 6 = 0$$

(3)

(b) Write down the solutions of

$$25r^2 - 25r - 6 = 0$$

(1)

Hence,

(c) state the value of r , giving a reason for your answer,

(1)

(d) find the sum of the first 4 terms of the series.

(2)



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Question 7 continued

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Question 7 continued

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Q7

(Total 10 marks)



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8. In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

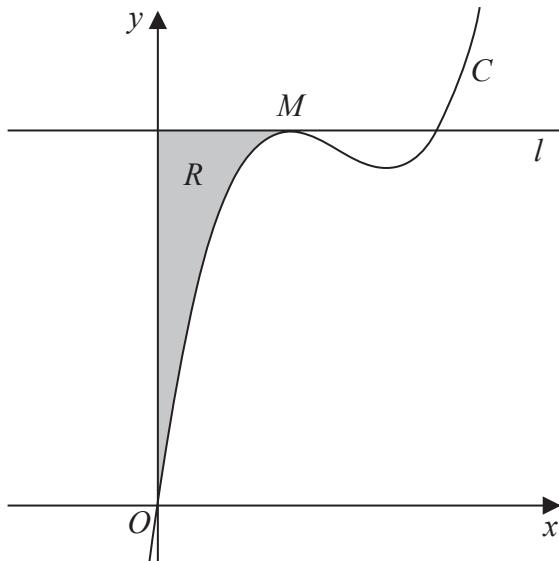


Figure 2

Figure 2 shows a sketch of part of the curve C with equation

$$y = \frac{4}{3}x^3 - 11x^2 + kx \quad \text{where } k \text{ is a constant}$$

The point M is the maximum turning point of C and is shown in Figure 2.

Given that the x coordinate of M is 2

- (a) show that $k = 28$

(3)

- (b) Determine the range of values of x for which y is increasing.

(2)

The line l passes through M and is parallel to the x -axis.

The region R , shown shaded in Figure 2, is bounded by the curve C , the line l and the y -axis.

- (c) Find, by algebraic integration, the exact area of R .

(5)



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Question 8 continued



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Question 8 continued

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Q8

(Total 10 marks)



P 6 9 1 9 9 A 0 2 7 3 2

9. (a) Prove that for all positive values of x and y ,

$$\frac{x+y}{2} \geq \sqrt{xy} \quad (3)$$

(b) Prove by counter-example that this inequality does not hold when x and y are both negative.

(1)

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Question 9 continued

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Q9

(Total 4 marks)



10. In this question you must show all stages of your working.

Solutions relying entirely on calculator technology are not acceptable.

(i) Solve, for $-\frac{\pi}{2} < x < \frac{\pi}{2}$

$$\tan^2\left(2x + \frac{\pi}{4}\right) = 3 \quad (5)$$

(ii) Solve, for $0 < \theta < 360^\circ$

$$(2 \sin \theta - \cos \theta)^2 = 1$$

giving your answers, as appropriate, to one decimal place.

(5)



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Question 10 continued

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Q10

(Total 10 marks)

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TOTAL FOR PAPER IS 75 MARKS

